On nonequilibrium shrinkage of supercritical CO$_2$ droplets in a water-carrier microflow

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We report an experimental study on the hydrodynamic shrinkage of supercritical carbon dioxide (scCO$_2$) microdroplets during a nonequilibrium process. After scCO$_2$ microdroplets are generated by water shearing upon a scCO$_2$ flow in a micro T-junction, they are further visualized and characterized at the midpoint and the ending point of a straight rectangular microchannel (width $\times$ depth $\times$ length: 150 $\mu$m $\times$ 100 $\mu$m $\times$ 1.5 mm). Measured decreases in droplet size by 8% ~ 36% indicate and simply quantify the droplet shrinkage which results from the interphase mass transfer between the droplet and the neighboring water. Using a mathematical model, the shrinkage of scCO$_2$ droplets is characterized by solvent-side mass transfer coefficient ($k_s$: $1.5 \times 10^{-4}$ ~ $7.5 \times 10^{-4}$ m/s) and the Sherwood number ($Sh$: 7 ~ 37). In general, $k_s$ here is two orders of magnitude larger than that of hydrostatic liquid CO$_2$ droplets in water. The magnitude of Sh numbers highlights the stronger effect of local convections than that of diffusion in the interphase mass transfer. Our results, as reported here, have essential implications for scCO$_2$-based chemical extractions and carbon storage in deep geoformations.

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Due to its liquid-like density (10s to 100s kg/m$^3$), gas-like viscosity (10 ~ 100 $\mu$Pa$\cdot$S), and intermediate diffusion coefficient ($10^{-9}$ ~ $10^{-7}$ m$^2$/s) at moderate conditions, among other properties (e.g., nontoxicity and nonflammability), supercritical CO$_2$ (scCO$_2$) is deemed one of the green solvents$^{1,2}$. In order to enhance mass transfer as well as reaction rates, processes involving scCO$_2$ have been tested in microfluidics for about a dozen years. Among these attempts, scCO$_2$ has been mostly used in chemical reactions as solvent$^3$ or a reactant$^4$ and in extractions of non-polar compounds or emulsions purely as solvent$^5$-$^7$. Besides, some physical properties of scCO$_2$, e.g., solubility$^8$, can be probed in microfluidic devices, analogous to that of gaseous CO$_2$ which receives much more attention.$^9$-$^{10}$ On the other hand, the environmental impact of CO$_2$ nowadays makes demands for mitigation solutions, e.g., carbon capture and storage (CCS) in which CO$_2$ is considered to be injected and stored at a supercritical state in deep geoformations. Due to a presence of resident water, injected fluid-phase CO$_2$ is very likely to form a partially miscible fluid pair with it within nano- to micro-scale pores and throats, and the formed interface is actually a binary mixture region (i.e., nonzero-thickness boundary) in view of the solubility and diffusivity of CO$_2$. In this case, an interphase mass transfer occurs that is mainly driven by dissolution, diffusion, and potential local convection. This mechanism (sometimes simply called “dissolution trapping”) of CO$_2$ storage assists in ensuring a secure carbon storage in a long term. Some experimental studies have reported the shrinkage of CO$_2$ bubbles or segments in contact with miscellaneous liquids.$^{11}$-$^{37}$ The interphase mass transfer between liquid CO$_2$ droplets and water as well as a resulted shrinkage has been investigated as well, suggesting a mass transfer coefficient of $10^{-7}$ ~ $10^{-6}$ m/s.$^{18}$-$^{20}$ Nevertheless, there are few studies of the shrinkage of scCO$_2$ droplets in contact with aqueous phases which indeed have essential implications for scCO$_2$ based extractions, reactions, and CO$_2$ storage.
Due to the chemical potential, shrinkage of scCO₂ droplets can be foreseen which is essentially a nonequilibrium process during an early stage of their contact.¹⁶ The nonequilibrium nature of the interphase mass transfer mainly lies in the fact that the microscopic concentration field of CO₂ in the binary region is time-dependent and susceptible to surrounding hydrodynamic and/or thermodynamic effects.²¹,²² Nevertheless, possible shrinkage of individual scCO₂ droplets, based on certain statistics, can be evaluated quantitatively, for example, using mass transfer coefficients.

In this Letter, the shrinkage of flowing scCO₂ droplets in a water-carrier microflow is reported. scCO₂ microdroplets are first generated at a T-junction microchannel with a rectangular cross-section (width × depth: 150 µm × 100 µm) in a silicon–glass microchip (74 mm × 44 mm × 1.2 mm) and then measured in terms of their length (Lₙ) and speed (vₙ) at specified positions (x) along a long straight channel, as shown by Fig. 1. An experimental setup (see Fig. S1 in the supplementary material and Ref. 23) for high-pressure microfluidic studies is utilized here to fulfill the experimental study. At the T-junction, pre-conditioned scCO₂ is dispersed from the side channel into the straight channel where DI water flows, shears, and squeezes off the CO₂ stream, forming scCO₂ microdroplets. Given an appropriate flow rate ratio (Q_{scCO₂}/Q_{H₂O}) of scCO₂ and water, the droplet generation at the T-junction becomes periodical and the size (L₁) of generated droplets is overall constant.²⁴ By comparing Lₓ at these three positions, the reduction in droplet length can be obtained. Generally, droplet visualization and measurement at each position are achieved by: (1) using a microscope (BX51, Olympus) equipped with a high speed camera (v210, Phantom) working with a rate of 3000 frames per second (fps), and (2) video analyses for Lₓ and vₓ using in-house developed Matlab (R2014a, Mathworks) codes based on identifying droplets and their centroids. For maintaining a supercritical state, CO₂ at its pump, in the facilitating stainless steel tubing (inner diameter: ~ 570 µm), and at the microchip are regulated beyond 8 MPa and at 40°C.

Two groups of Q_{scCO₂}/Q_{H₂O} are investigated: (1) 10/90 ≤ Q_{scCO₂}/Q_{H₂O} ≤ 75/25, and Q_{scCO₂} + Q_{H₂O} = 100 µL/min; and (2) 50/280 ≤ Q_{scCO₂}/Q_{H₂O} ≤ 50/100, and Q_{scCO₂} = 50 µL/min. Note that the minimum and the maximum ratio applied here are a lower and an upper limit rendering observable scCO₂ droplet flows at the micro T-junction with an imaging area of 1600 µm × 400 µm. The capillary number (Caₙ = ηᵥ/v/γ) of the continuous phase (i.e., DI water) at the T-junction is calculated, ranging from 1.1 × 10⁻³ to 1.2 × 10⁻², where the viscosity, ηᵥ = 655.5 µPa·s²⁵ and interfacial tension, γ = 33.5 mN·m⁻¹ ²⁶,²⁷ are referred to those at a temperature of 313 K and a pressure of 7776 ~ 7940 kPa, and the characteristic velocity, vᵥ, is determined by vᵥ = Q_{H₂O}/(WD/2) by assuming water occupies a half width of the channel on average. The generation of scCO₂ droplets is mostly in a squeezing regime in which the interfacial tension dominates over the shear stress. Despite this, a transition to a dripping regime where shear stresses become important is anticipated as the water flow reaches 200 µL/min leading to Caᵥ ~ 0.01²⁸. By then, the injected scCO₂ stream is unable to touch with the channel wall and very small droplets (Lₓ/W ≤ 2) are produced.

Figure 2(a) and (b) provides a collection of snapshots of the representative scCO₂ microdroplet at each of the three positions and...
shows a nondimensionalized size \((L/W)\) as well as an overall relative shrinkage of the scCO2 droplet. \(L/W\) can be linearly correlated to \(Q_{scCO2}/Q_{H2O}\) in a T-junction with its geometry known, and \(L/W = 1 + \alpha (Q_{scCO2}/Q_{H2O})\) according to Garstecki et al.\textsuperscript{24}

It’s found in this study that \(\alpha \approx 3.6\) for \(Q_{scCO2} + Q_{H2O} = 100 \mu L/min\) \((0.1 < Q_{scCO2}/Q_{H2O} < 2.3)\) and \(\alpha \approx 2.0\) for \(Q_{scCO2} = 50 \mu L/min\) \((0.2 < Q_{scCO2}/Q_{H2O} < 0.5)\).

FIG. 2. Overview of scCO2 droplets at three positions for the group (a) \(Q_{scCO2} + Q_{H2O} = 100\mu L/min\) and (b) \(Q_{scCO2} = 50\mu L/min\). (c) Dimensionless droplet length \(L/W\) \((x = 1\) (circles), 2 (down triangles) or 3 (up triangles)). (d) Overall relative droplet shrinkage \(\Delta L/L\) \((\Delta L = L_1 - L_3)\). In (c) and (d), solid and open symbols are corresponding to (a) and (b), respectively.

respectively, both are greater than 1. In fact, simultaneous squeezing and dragging effects of water over the interface, leading to the pinch-off of the scCO2 stream at the junction, have extended the truncation time for droplets. Thus it amplifies the contribution of \(Q_{scCO2}\) relative to \(Q_{H2O}\) in increasing the size of the emerging droplet. Notably, the smaller \(\alpha\) for the latter group is due to increased shear effects as \(Q_{H2O}\) increases and accelerates the droplet formation. By comparing \(L/W\) at a specific \(Q_{scCO2}/Q_{H2O}\), a decreasing trend from position 1 to 2 and down to 3 exists, i.e., \(L_1/W > L_2/W > L_3/W\), and is applicable to the two groups of \(Q_{scCO2}/Q_{H2O}\) [see Fig. 2(c)]. This trend simply indicates the shrinkage of scCO2 microdroplets. The shrinkage is a result of the interphase mass transfer of CO2 molecules driven by a synergic dissolution-diffusion mechanism due to CO2 solubility in water and a consequent concentration gradient of CO2. Besides, local convections near the interface are able to accelerate the mass transfer by continuously refreshing the solvent.\textsuperscript{29,30} The overall shrinkage can be divided into two stages, \(\Delta L_1 = L_1 - L_2\) and \(\Delta L_2 = L_2 - L_3\). It is found that \(\Delta L_1 \geq \Delta L_2\) generally applies to the cases of \(Q_{scCO2}/Q_{H2O} \leq 1\). It means that a rapid shrinkage occurs during the early stage of the droplet flow. Similar behaviors of CO2 bubbles are reported by Shim \textit{et al.}\textsuperscript{16} and an early rapid dissolution regime and a subsequent equilibrium regime are identified. During the early stage, dissolution controls the shrinkage prior to saturation. Later, diffusion and convection start to manifest since saturation is achieved at the near-CO2 boundary of the binary mixture zone where diffusion is kinetically slower. Thus, shrinkage during later time is less. Besides, \(\Delta L_1\) almost equals to \(\Delta L_2\) when \(Q_{H2O} > 100 \mu L/min\) [see an inset in FIG. 2(c)], implying that dissolution is still dominant given that the residence time of scCO2 droplets in the channel is much shortened. However, a clear distinction of \(\Delta L_1\) from \(\Delta L_2\) is not observed for \(Q_{scCO2}/Q_{H2O} > 1\) [see Fig. 2(c)] due to the deviation of \(L_s\). \(\Delta L\) of droplets at \(Q_{scCO2} + Q_{H2O} = 100 \mu L/min\) are averaged as \((115 \pm 3.4)\ \mu m\). but varies nearly linearly from 86 to 20 \(\mu m\) as \(Q_{scCO2}/Q_{H2O}\) tuned from 50/100 to 50/280. The shrinkage may be considered in a relative way in terms of \(\Delta L/L_1\) [see Fig. 2(d)]. For the group \(Q_{scCO2} + Q_{H2O} = 100 \mu L/min\), increasing \(Q_{scCO2}/Q_{H2O}\) leads to decreasing \(\Delta L/L_1\) from 35% to <10% almost linearly. However, the interrelation is reverse for \(Q_{scCO2} = 50 \mu L/min\). These reveal \(\Delta L\) is closely related to the flowing time of droplets in the channel that can be quantified using droplet speeds.

Analogous to \(L_s\), droplet speed \(v_s\) \((x = 1, 2, or 3)\) is measured at all three positions and presented in Fig. S3 in the supplementary material. For the group \(Q_{scCO2} + Q_{H2O} = 100 \mu L/min\), \(v_s\) is \~100 mm/s at various \(Q_{scCO2}/Q_{H2O}\) despite variations at the three positions and different variation behavior at different \(Q_{scCO2}/Q_{H2O}\) (relevant discussions are provided in the supplementary material). For the group \(Q_{scCO2} = 50 \mu L/min\), \(v_s\) increases linearly.
from ~120 to ~360 mm/s on average as $Q_{scCO2}/Q_{H2O}$ tuned from 50/100 to 50/280. When $v_x$ reaches 300 mm/s at $Q_{scCO2}/Q_{H2O} < 50/200$, the flowing time ($t_f$, ms) of droplets becomes very short (~50 ms) leading to very subtle droplet shrinkage [see the inset in Fig. 2(c)]. In order to evaluate the flowing time, $v_x$ are averaged to a characteristic droplet speed ($\bar{v}$) for each flow case. $\bar{v}$ and $t_f$ are calculated \[\bar{v} = (\sum_{x=1}^{3} v_x)/3 \] and \[t_f = L_f / \bar{v} \] and shown in Fig. S4. By using $L_x$ and $t_f$, the solvent-side mass transfer coefficient $k_s$ that characterizes the hydrodynamic shrinkage of scCO$_2$ droplets can be determined. Starting from a differential form of $k_s [k_s = \frac{C_s}{C_e} d(V) / \Delta t]$ in an infinitesimal time step, we obtained a specific form of $k_s$ (see detailed derivations in Section S5 in the supplementary material) by accounting for a typical Taylor droplet in a rectangular microchannel at a 3D scenario and based on rewriting the surface area ($A$, m$^2$) and volume ($V$, m$^3$) of the droplet in terms of readily available parameters (e.g., $W$, $D$, $L_o$), as follows

\[k_s (mm/s) = \frac{(0.96WD-0.0632W^2)}{(1.548W+2D)} \frac{C_d}{C_e} \left( \ln \frac{A_0}{A_x} \right)^{1/3} \t^2, \quad (1)\]

where $C_d$ and $C_e$ are a nominal “molar concentration” ($C_d = \rho_{scCO2}/M$, mol/L) of CO$_2$ and the solubility of CO$_2$ in water, respectively. The term $\Delta C = C_e - C_0$ (the surrounding CO$_2$ concentration $C_0 \approx 0$) in denominator refers to a driving concentration difference for the water-side mass transfer. For calculating $A$, the contact angle [$\theta_c = (141 \pm 1.2)^\circ$] between droplet and water at the channel wall averaged from all imaging frames is applied. In order to calculate $k_s$, $C_d$ is determined by $\rho_{scCO2}$ and the molar mass $M$, and $C_e [(1.153 \pm 0.005)$ mol/L] is referred to that at 313 K and a pressure of 8185 ~ 8284 kPa. \(^{31,32}\)

To assist with discussions, we performed a simple CFD study of a single flowing (100 mm/s) scCO$_2$ droplet with water in the long straight microchannel as the computational domain. A VOF (volume-of-fluid) method based on a fraction function of the two phases is adopted in CFD software Fluent (version 17, Ansys Inc.). In addition, an overall continuity and a momentum equation as well as a continuum surface (force) tension model and the contact angle ($\theta_c$) are applied. Fluid properties (density and viscosity of water and that as well as diffusivity of scCO$_2$) are considered by referring to aforementioned pressures and temperature. Flow streamlines (after subtracting a superficial velocity of 100 mm/s

\[FIG. 3. (a) Mass transfer coefficient $k_{s,1-3}$ and (b) Sherwood numbers. In (a) and (b), solid symbols: $Q_{scCO2} + Q_{H2O} = 100 \mu L/min$; hollow symbols: $Q_{scCO2} = 50 \mu L/min$. Error bar indicates one standard deviation according to error propagation. Fitting lines are added for discussions only. (c) A snapshot of a flowing (~100 mm/s, from left to right) scCO2 droplet at position 2 in the channel. (d) Numerically computed flow streamlines within the flowing droplet (red colored) and water slugs (white regions) near the meniscus. Local convections represented by vortexes are detailed in magnified views in (e) and (f). For reference, the magnitude of water velocity near the droplet meniscus is ~30 mm/s.\]

$k_s$ are calculated by $L_1$, $L_3$, and $t_f$ and shown in FIG. 3(a). Note that $k_{s,1-3}$ here is a convective mass transport coefficient\(^{33}\) accounting for the hydrodynamics within both the droplet and the water slug as well as in the vicinity of the droplet meniscus. Based on the CO$_2$ diffusivity ($D_{dc} \approx 1.5 \times 10^{-9}$ m$^2$/s)\(^{34}\) in water at the experimental condition and a half channel width as a characteristic length ($L_{mass} = W/2$) for the mass transfer, the Sherwood number [\(Sh = k_{s,1-3}/(D_{dc}/L_{mass})\)] that compares the strength of the convective mass transfer with that of diffusion can be determined, as shown in FIG. 3(b).
from the domain) within the droplet and water corresponding to the moment when droplet arrives at position 2 [see FIG. 3(d), (e), and (f)] reveal that toroidal vortexes are formed within the droplet and the water region close to the droplet meniscus. The convective hydrodynamics near the droplet meniscus dominate in transporting CO$_2$ by continuously refreshing the meniscus region and bringing away dissolved CO$_2$.

As shown in FIG. 3(a) and (b), a negative logarithmic relation is found for both $k_s$ and the $Sh$ number with $Q_{scCO2}/Q_{H2O}$. Same relations between these two parameters and $L_d/W$ may exist as well in view of a linear correlation of $Q_{scCO2}/Q_{H2O}$ and $L_d/W$. For a small scCO$_2$ droplet (i.e., small $L_d/W$), it presents better mass transfer (higher $k_s$) and enhanced dominance of convection over diffusion in controlling the mass transport of CO$_2$ (larger $Sh$). This disparity is highlighted as well for the same $Q_{scCO2}/Q_{H2O}$ but with an increased $Ca_e$ that results in even smaller CO$_2$ droplets. Generally, small droplets feature a larger effective portion of an overall interfacial region for the mass transfer and this convection-featured portion contributes more in the mass transport. Moreover, as droplets have a comparably small size, increased $Ca_e$ indicating enhanced shear effects relative to interfacial tension strengthens the convection in the vicinity of the droplet meniscus that promotes the mass transport further.

In conclusion, we have experimentally reported on the shrinkage of flowing scCO$_2$ microdroplets in a water-carrier flow in a straight microchannel. Using a micro T-junction, scCO$_2$ droplets (surface-to-volume ratios ~ 33.2 mm$^{-1}$) are produced by applying a series of $Q_{scCO2}/Q_{H2O}$ and their length, speed, and the flowing time are either measured or calculated. A mathematical model of the solvent-side mass transfer coefficient ($k_s$) is developed by accounting for the 3D morphology of a typical Taylor droplet in a rectangular microchannel. $k_s$ in our work ranges from $1.5 \times 10^{-4}$ to $7.5 \times 10^{-4}$ m/s which is two orders of magnitude higher than that of the hydrostatic liquid CO$_2$ droplets in water$^{18-20}$. The $Sh$ (7 ~ 37) number reveals the dominance of convections over diffusion in controlling the mass transfer. These findings highlight the benefits of using scCO$_2$ and small droplets in a hydrodynamic scenario when it comes to applications of CO$_2$ in chemical processes and deep underground or oceanic CO$_2$ storage.

See supplementary materials for a schematic of the experimental setup, measurements of droplet length and speed, and a detailed development of the mathematical model of the solvent-side mass transfer coefficient.

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