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Inverse Dynamics Modelling of Paralympic Wheelchair Curling

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28 **Abstract**

29 Paralympic wheelchair curling is an adapted version of Olympic curling played by individuals with spinal
30 cord injuries, cerebral palsy, multiple sclerosis, and lower extremity amputations. To the best of the
31 authors' knowledge, there has been no experimental or computational research published regarding the
32 biomechanics of wheelchair curling. Accordingly, the objective of this research was to quantify the angular
33 joint kinematics and dynamics of a Paralympic wheelchair curler throughout the delivery. The angular joint
34 kinematics of the upper extremity were experimentally measured using an inertial measurement unit
35 system; the translational kinematics of the curling stone were additionally evaluated with optical motion
36 capture. The experimental kinematics were numerically optimized to satisfy the kinematic constraints of a
37 subject-specific multibody biomechanical model. The optimized kinematics were subsequently used to
38 compute the resultant joint moments via inverse dynamics analysis. The main biomechanical demands
39 throughout the delivery (i.e., in terms of both kinematic and dynamic variables) were about the hip and
40 shoulder joints, followed sequentially by the elbow and wrist. The implications of these findings are
41 discussed in relation to wheelchair curling delivery technique, musculoskeletal modelling, and forward
42 dynamic simulations.

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53 **Keywords:** multibody dynamics, biomechanical modelling, kinematic constraints, inertial measurement
54 units, optical motion capture, sports biomechanics

55 **Introduction**

56 Wheelchair curling debuted at the 2006 Paralympic Games. Competing athletes utilize the same stones
57 and ice sheets as Olympic curlers, although sweeping (i.e., using a broom to control the stone's
58 trajectory) is omitted and the stone must be pushed from a stationary wheelchair using a delivery stick.¹
59 One of the main objectives in wheelchair curling is to launch the stone in such a way that it rectilinearly
60 translates along the ice over 28 m and lands within the 'house' to accumulate points; this is known as a
61 'draw shot' delivery. Research conducted at the 2010 Paralympic Games noted that 18 % of athletes
62 competing in wheelchair curling ($n = 50$) sought medical attention for musculoskeletal injuries, the
63 majority of which were sustained about the lower back and shoulder joint.² To date, there has been no
64 experimental or computational research published regarding the biomechanics of wheelchair curling.
65 These investigations would provide unprecedented insights into the physical demands of this Paralympic
66 sport.

67 One of the main objectives of biomechanists is to evaluate the dynamics (i.e., forces and
68 moments) associated with human movements. Experimentally measuring the forces of individual skeletal
69 muscles (i.e., dynamometry) is invasive and therefore unpractical in sport environments.³ With modern
70 advancements in computer science, biomechanical modelling presents a viable method of approximating
71 the dynamics of multibody movements.³ Considering the emergent interests in determining the physical
72 demands of different Paralympic sports, the objectives of this research were i) to develop a subject-
73 specific multibody biomechanical model of Paralympic wheelchair curling, and ii) to quantify the angular
74 joint kinematics and dynamics throughout the wheelchair curling delivery via experimental measurements
75 and inverse dynamics analysis, respectively.

76 **Methods**

77 **Paralympic Athlete**

78 A single wheelchair curler (sex: male, age: 39 y, total body mass: 87.9 kg) was recruited from the
79 Canadian Paralympic Team. The athlete was a gold medalist at the 2014 Paralympic Games and 2013
80 World Wheelchair Curling Championships. In 2007, the athlete sustained a traumatic incomplete spinal

81 cord injury between the 5th and 6th cervical vertebrae. The athlete was diagnosed with a level 'C'
82 impairment on the American Spinal Injury Association Impairment Scale.⁴ The Paralympian provided
83 informed written consent and the University of Waterloo Research Ethics Board approved this research.

84 **Experimental Kinematics**

85 The angular joint kinematics throughout the wheelchair curling delivery were experimentally measured
86 using an inertial measurement unit (IMU) system (MVN Suit, Xsens Technologies, Netherlands). The
87 system consists of 17 IMUs, which were attached to the Paralympian's head, torso, upper arms,
88 forearms, hands, thighs, shanks, and feet (Figure 1). The IMU system utilises a 23-segment
89 biomechanical model and proprietary algorithms to calculate the angular joint kinematics.⁵ The
90 Paralympian performed 14 'draw shot' deliveries of the curling stone interspersed with 2 minutes of rest
91 between deliveries; all 14 deliveries were considered in the analyses. The athlete used his right hand to
92 deliver the curling stone. Data were sampled at 120 Hz. High-frequency noise in the joint kinematic
93 measurements was minimized using smoothing splines (MATLAB, MathWorks, USA). Previous research
94 has demonstrated the test-retest reliability⁶ and concurrent validity⁷ of the IMU system in computing
95 angular joint kinematics compared with optical motion capture.

96 Movement of the curling stone was recorded with a digital camera (Nikon D3100, Nikon
97 Corporation, Japan) that was positioned perpendicular to the Paralympian's plane of motion. The camera
98 sampled at 29 frames per second. The translational stone kinematics (i.e., displacements and velocities)
99 throughout the delivery were determined relative to an inertial reference frame using markerless feature
100 tracking software (ProAnalyst, Xcitex Incorporation, USA). The delivery is defined as the time duration
101 between the initial displacement of the stone and its moment of release from the delivery stick. High-
102 frequency noise in the stone kinematic measurements was minimized using smoothing splines (MATLAB,
103 MathWorks, USA).

104 **Multibody Biomechanical Model**

105 A novel biomechanical model of the wheelchair curling delivery was developed in MapleSim software
106 (MapleSoft, Canada). The model included a representative torso, head and neck, right upper arm, right

107 forearm, right hand, delivery stick, and curling stone (Figure 2a). The wheelchair is fixed to the inertial
 108 reference frame (Figure 2a). The mechanical parameters of each biological body segment were
 109 experimentally measured using dual-energy x-ray absorptiometry (Table 1).⁸ Synonymous with the
 110 Paralympian's equipment configuration, the delivery stick body segment was set to 1.96 m in length, 0.18
 111 kg in mass, and the principal mass moment of inertia was calculated via $I_{zz} = \frac{1}{12}mL^2$. The curling stone
 112 body segment was given a mass of 19.96 kg and a height of 0.19 m.⁹

113 The model also included a representative hip, shoulder, elbow, and wrist, all of which were
 114 modelled as revolute kinematic pairs (Figure 2b). The hip, shoulder, and elbow permit flexion-extension
 115 while the wrist allows for radial-ulnar deviation, assuming a neutral hand position (Figure 2b). The hip joint
 116 was set to 0.62 m above the inertial reference frame (i.e., simulating the height of the wheelchair seat)
 117 (Figure 2b). The revolute joints contained angular viscous damping, the quantities of which were taken
 118 from previous research.¹⁰⁻¹¹ A prismatic kinematic pair was used to model the contact between the curling
 119 stone and ice (Figure 2b); rotations about the vertical axis were omitted. The contact model also included
 120 dry Coulomb friction.⁹ The multibody biomechanical model has 3 degrees of freedom and is
 121 mathematically represented by 4 ordinary differential equations and 1 algebraic equation (i.e., indicative
 122 of the model's kinematic constraints).

123 Kinematic Constraints

124 The experimental kinematics were numerically optimized to satisfy the kinematic constraints of the
 125 multibody biomechanical model. A nonlinear constrained optimization algorithm was used to minimize the
 126 following multi-objective function at discrete time steps (i.e., $t = 0 \dots 0.65$ s and Δt resampled = 0.001 s)

$$127 \psi_t^\dagger = \text{Arg min} \left[\sum_{i=1}^5 w_i \left(\frac{\psi_{it} - \psi_{it}^m}{\Delta \psi_{it}^m} \right)^2 + w_6 \left(\frac{AE(\theta_{1t} \dots \theta_{4t})}{L} \right)^2 + w_7 \left(\frac{x_t - f(\theta_{1t} \dots \theta_{4t})}{\Delta x^m} \right)^2 \right] \quad (1)$$

$$128 \text{ subject to: } \psi_{min}^m < \psi_t < \psi_{max}^m \quad (2)$$

129 where $\psi = [\theta_1 \ \theta_2 \ \theta_3 \ \theta_4 \ x]^T$, ψ^m represents the experimentally measured ψ variables, $W_1 \dots W_7$ are
 130 weighting terms (i.e., $W_1 = 15$, $W_2 = 0.1$, $W_3 = 0.95$, $W_4 = 1.5$, $W_5 = 200$, $W_6 = 100$, and $W_7 = 100$), AE
 131 $(\theta_{1j} \dots \theta_{4j})$ is the algebraic constraint equation from the multibody biomechanical model, and L (i.e., 0.43 m)

132 is the vertical distance between the heights of the wheelchair seat and curling stone handle. $f(\theta_1 \dots \theta_4)$
133 denotes the modelled displacement (x) of the curling stone in terms of the variables $\theta_1 \dots \theta_4$. Equation (2)
134 specifies the minimum and maximum bounds on each ψ variable. The Paralympian's maximum range of
135 motion about the hip (θ_1), shoulder (θ_2), elbow (θ_3), and wrist (θ_4) were experimentally measured using a
136 digital goniometer. $\Delta\psi$ is the difference between ψ_{min}^m and ψ_{max}^m .

137 **Inverse Dynamics**

138 Inverse dynamics is a mathematical technique through which resultant forces and moments about
139 individual joints are calculated by solving the Newton-Euler equations of motion given the kinematics and
140 inertial parameters of adjacent body segments.³ The MapleSim software was used to solve the Newton-
141 Euler equations of motion for the resultant joint moments about the hip, shoulder, and elbow using the
142 optimized kinematics. The wrist was modelled as a passive joint (i.e., unactuated) in the interests of
143 simulating the limited hand functionality of the Paralympic wheelchair curler.

144 **Results**

145 The shoulder joint displayed the largest range of motion (i.e., $\Delta 142.7 \pm 3.1^\circ$) throughout the wheelchair
146 curling delivery compared to the hip (i.e., $\Delta 27.0 \pm 2.9^\circ$), elbow (i.e., $\Delta 96.7 \pm 3.3^\circ$), and wrist (i.e., $\Delta 22.8$
147 $\pm 1.7^\circ$) (Figure 3). The mean duration of the delivery was approximately 0.65 seconds. The delivery was
148 initiated through rotations about the hip (i.e., flexion), followed sequentially by the shoulder (i.e., flexion),
149 elbow (i.e., extension), and wrist (i.e., ulnar deviation).

150 The shoulder joint had the largest magnitude of angular velocity throughout the delivery, with a
151 maximum flexion velocity of 427.2 ± 12.6 °/s and extension velocity of -4.1 ± 16.4 °/s (Figure 4). The hip
152 joint had a maximum flexion velocity of -133.8 ± 10.2 °/s (Figure 4). The elbow joint had a maximum
153 flexion velocity of 21.0 ± 13.3 °/s and extension velocity of -299.7 ± 16.7 °/s (Figure 4). The wrist joint had
154 a maximum radial-deviation velocity of 17.2 ± 9.6 °/s and ulnar-deviation velocity of -126.3 ± 12.1 °/s
155 (Figure 4).

156 There was minimal translational stone acceleration just before the moment of release (Figure 5);
157 this technique is presumably used by the Paralympian to enhance precision. The translational release
158 velocity (i.e., 2.0 ± 0.1 m/s) correlated with that reported by recent mathematical models of curling stone
159 mechanics.⁹ The uncertainties in the translational stone velocities slightly increased as a function of the
160 duration of the delivery (Figure 5). The curling stone displaced a maximum of 0.80 ± 0.02 m throughout
161 the delivery (Figure 5). The Paralympian exhibited a high degree of inter-delivery consistency, as
162 evidenced by the minor uncertainties in the stone kinematics (Figure 5).

163 The largest joint moments throughout the wheelchair curling delivery were about the hip joint (i.e.,
164 maximum of 203.2 ± 34.9 Nm), followed by the shoulder (i.e., maximum of 54.6 ± 6.2 Nm) and elbow (i.e.,
165 maximum of 12.6 ± 2.2 Nm) (Figure 6).

166 **Discussion**

167 The objectives of this research were i) to develop a subject-specific multibody biomechanical model of
168 Paralympic wheelchair curling, and ii) to quantify the angular joint kinematics and dynamics throughout
169 the wheelchair curling delivery via experimental measurements and inverse dynamics analysis,
170 respectively. The main kinematic demands throughout the delivery (i.e., in terms of maximum range of
171 motion and angular velocity) were about the shoulder joint; this may explain why previous research found
172 the highest incidences of musculoskeletal injuries in Paralympic wheelchair curling were about the
173 shoulder.² The Paralympian initiated the delivery via forward hip flexion, followed sequentially by shoulder
174 flexion, elbow extension, and ulnar-deviation. This kinematic sequencing resembles a 'follow-through'
175 technique. The Paralympian's delivery technique was also highly reproducible, as evidenced by the minor
176 uncertainties in the joint (Figures 3-4) and stone (Figure 5) kinematics. To the best of the authors'
177 knowledge, these findings represent the first documented kinematic analysis of the wheelchair curling
178 delivery. Although the joint kinematics might be considered indicative of an 'optimal' delivery technique
179 (i.e., since the athlete is a Paralympic gold medalist), additional research is needed to ascertain the
180 delivery kinematics of other Paralympic wheelchair curlers to derive statistically significant conclusions.

181 The multibody biomechanical model was used to evaluate the resultant joint moments about the
182 lower back and upper extremity joints throughout the wheelchair curling delivery. Resultant joint moments
183 are mathematical summations of the dynamics from all neighbouring biological elements (e.g., skeletal
184 muscles, tendons, ligaments, and bursae).³ Consequently, the forces and moments from individual
185 skeletal muscles cannot be determined. For example, the positive resultant joint moment about the elbow
186 joint throughout the wheelchair curling delivery (Figure 6) could be attributed to either activations of the
187 agonist muscles (e.g., biceps brachii) or deactivations of the antagonist muscles (e.g., triceps brachii).
188 Musculoskeletal models would be needed to evaluate the activations and dynamics of individual skeletal
189 muscles throughout the wheelchair curling delivery. These models could provide further insights into the
190 documented musculoskeletal injuries amongst Paralympic wheelchair curlers.²

191 Considering a wide variety of individuals with physical disabilities compete in wheelchair curling,
192 including those with spinal cord injuries, cerebral palsy, multiple sclerosis, and lower extremity
193 amputations,¹ it is important to quantify the maximum physical demands associated with the delivery
194 movement. The resultant joint moments throughout the wheelchair curling delivery were calculated using
195 inverse dynamics analysis. The maximum dynamic loads were computed about the hip joint, followed
196 sequentially by the shoulder and elbow. Nevertheless, inverse dynamics is not predictive, and requires
197 expensive and time-consuming experiments. Forward dynamics, by contrast, computes the multibody
198 kinematics by numerically integrating the Newton-Euler equations of motion given the forces and
199 moments as inputs; these dynamic inputs are often elicited from mathematical models of neural
200 excitations.³ Forward dynamics has the distinct capability of i) predicting the effects of model parameters
201 (e.g., height of the wheelchair seat) on performance outcomes, and ii) optimizing equipment designs *in*
202 *silico*.¹² Consequently, the authors intend to further investigate the biomechanics of wheelchair curling
203 using forward dynamic simulations.

204 **Acknowledgments**

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208 **Conflict of Interest**

209 The authors declare that they have no conflict of interest.

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210 **References**

- 211 1. World Curling Federation. The Rules of Curling and Rules of Competition.
212 <http://www.worldcurling.org/rules-and-regulations>. Published October 2015. Accessed May 2016.
- 213 2. Webborn N, Willick S, Emery CA. The injury experience at the 2010 Winter Paralympic Games. *Clinical*
214 *Journal of Sports Medicine*. 2012;22:3-9.
- 215 3. Roberston DGE, Caldwell GE, Hamill J, Kamen G, Whittlesey SN. *Research Methods in Biomechanics*.
216 2nd ed. Champaign, USA: Human Kinetics; 2014.
- 217 4. Kirshblum SC et al. International standards for neurological classification of spinal cord injury (Revised
218 2011). *Journal of Spinal Cord Medicine*. 2011;34:535-546.
- 219 5. Roetenberg D. *Inertial and Magnetic Sensing of Human Motion*. [PhD Dissertation]. Enschede, The
220 Netherlands: University of Twente; 2006.
- 221 6. Cloete T, Scheffer C. Repeatability of an off-the-shelf, full body inertial motion capture system during
222 clinical gait analysis. *Proceedings of the IEEE 32nd Annual International Conference of the Engineering in*
223 *Medicine and Biology Society*. 2010: 5125-5128.
- 224 7. Zhang JT, Novak AC, Brouwer B, Li Q. Concurrent validation of Xsens MVN measurement of lower
225 limb joint angular kinematics. *Physiological Measurement*. 2013;34:63-69.
- 226 8. Laschowski B, McPhee J. Body segment parameters of Paralympic athletes from dual-energy X-ray
227 absorptiometry. *Sports Engineering*. 2016;19:155-162.
- 228 9. Maeno N. Dynamics and curl ratio of a curling stone. *Sports Engineering*. 2014;17:33-41.
- 229 10. Lebedowska MK. Dynamic properties of human limb segments. In: Karwowski W, ed. *International*
230 *Encyclopaedia of Ergonomics and Human Factors*. 2nd ed. Boca Raton, USA: CRC Press; 2006:315-
231 319.

- 232 11. Rapoport S, Mizrahi J, Kimmel E, Verbitsky O, Isakov E. Constant and variable stiffness and damping
233 of the leg joints in human hopping. *Journal of Biomechanical Engineering*. 2003;125:507-514.
- 234 12. Balzerson D, Banerjee J, McPhee J. A three-dimensional forward dynamic model of the golf swing
235 optimized for ball carry distance. *Sports Engineering*. 2016. doi:10.1007/s12283- 016-0197-7.

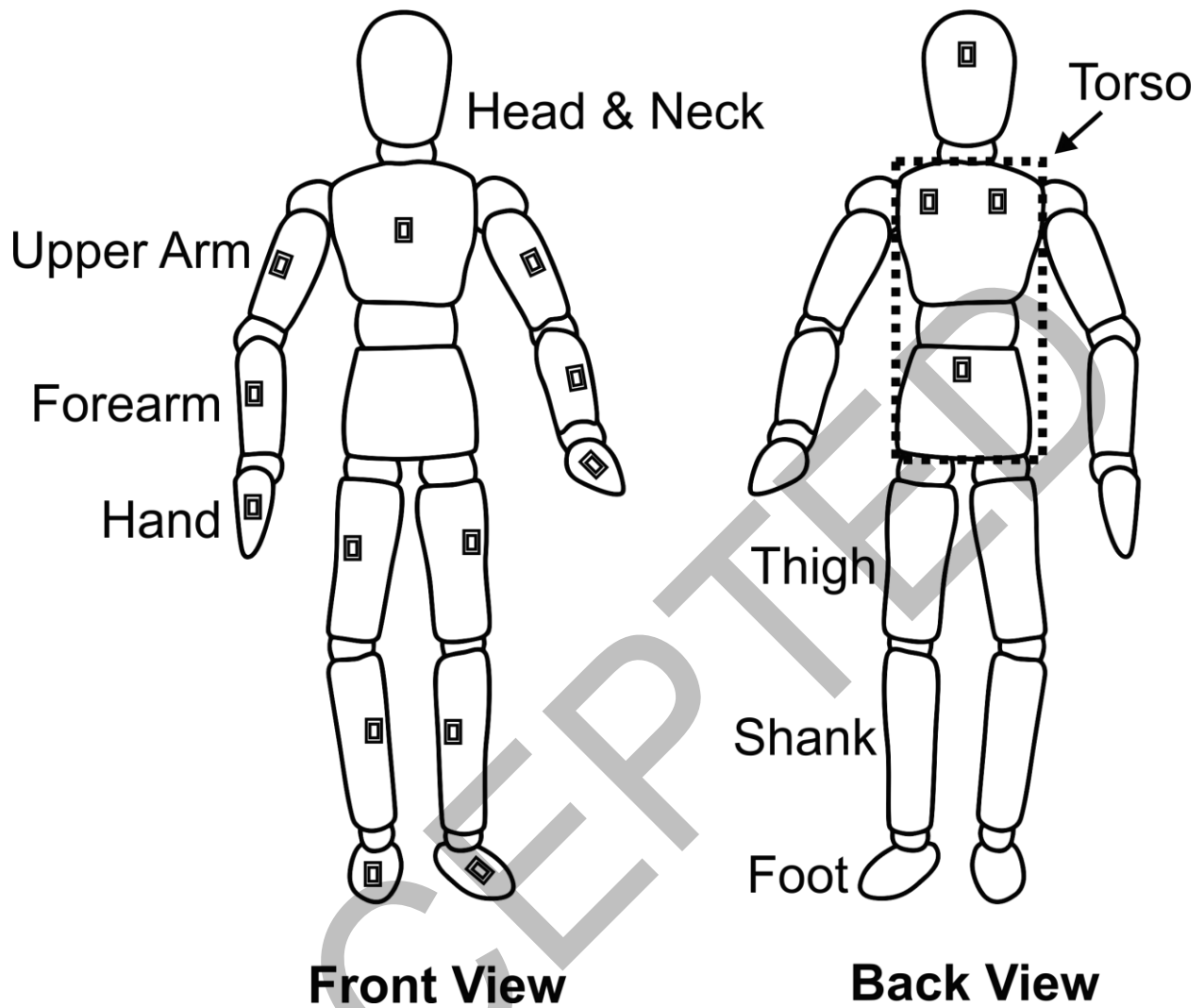
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236 **Table 1.** Body segment parameters of the Paralympic wheelchair curler as experimentally measured
 237 using dual-energy x-ray absorptiometry.⁸ The quantities are presented as arithmetic means \pm 1 standard
 238 deviation over multiple scans. Segments in the upper extremity are of the right side. The position vector of
 239 the center of mass was determined relative to the proximal endpoint.

Parameter	Head & Neck	Torso	Upper Arm	Forearm	Hand
Length (m)	0.265 \pm 0.005	0.588 \pm 0.008	0.291 \pm 0.005	0.276 \pm 0.002	0.123 \pm 0.002
Mass (kg)	6.967 \pm 0.085	44.616 \pm 0.677	3.099 \pm 0.192	1.371 \pm 0.009	0.396 \pm 0.011
Center of Mass (m)	0.1231 \pm 0.0025	0.2237 \pm 0.0031	0.149 \pm 0.002	0.108 \pm 0.001	0.022 \pm 0.001
Mass Moment of Inertia (kg·m ²)	0.1963 \pm 0.0102	2.8508 \pm 0.0349	0.0238 \pm 0.0022	0.0106 \pm 0.0002	0.0022 \pm 0.0001

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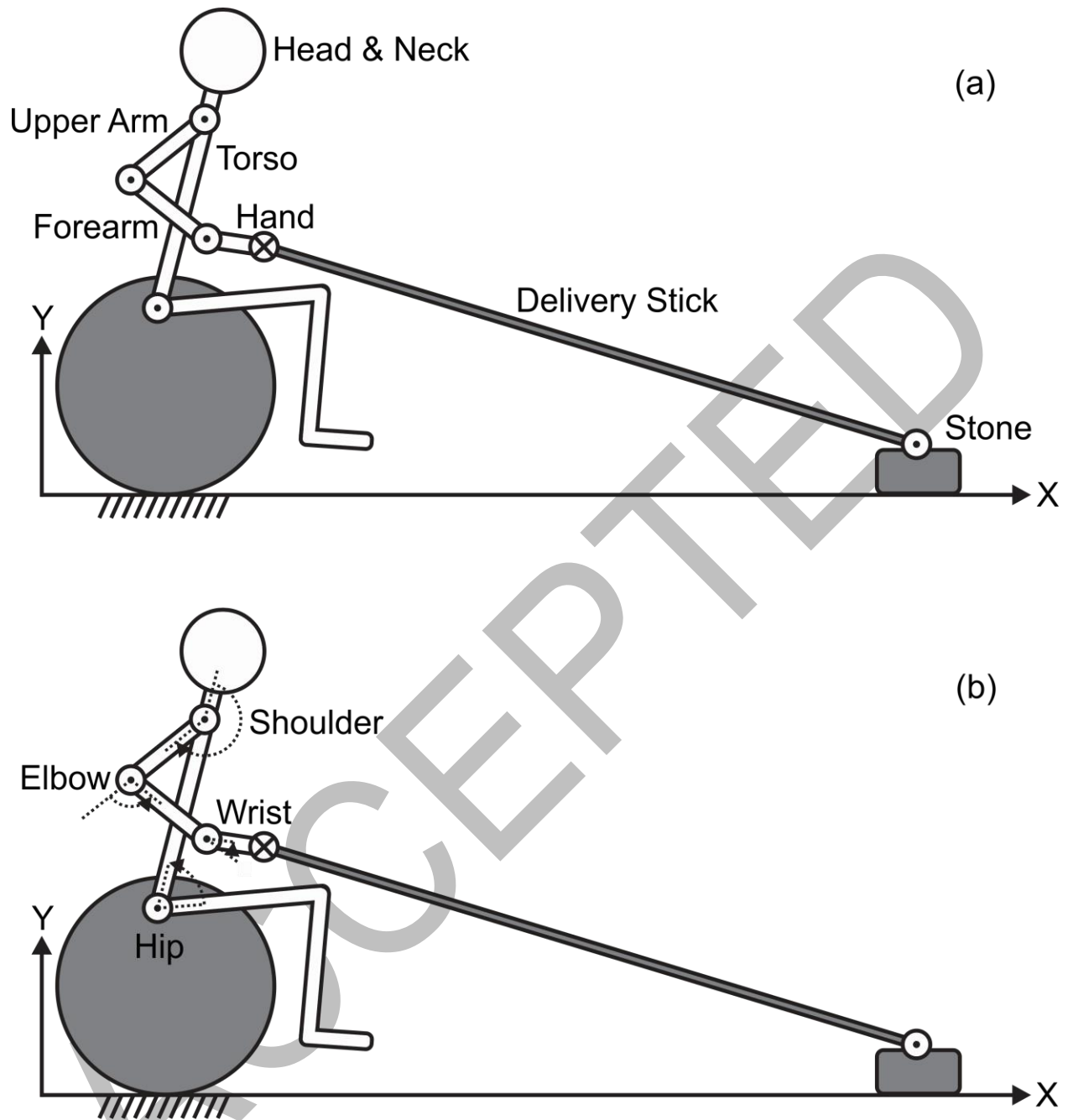
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Figure 1 – Locations of the inertial measurement units on the Paralympic wheelchair curler.

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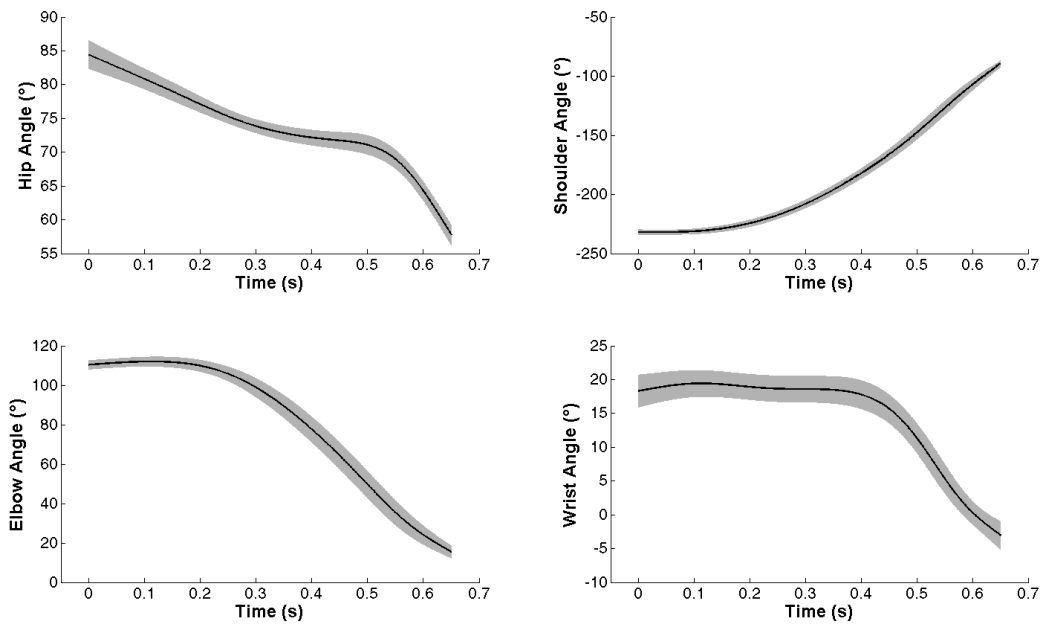
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 249 **Figure 2** - Schematic of the multibody biomechanical model. The rigid body segments and lower
 250 kinematic pairs are presented in (a) and (b), respectively.

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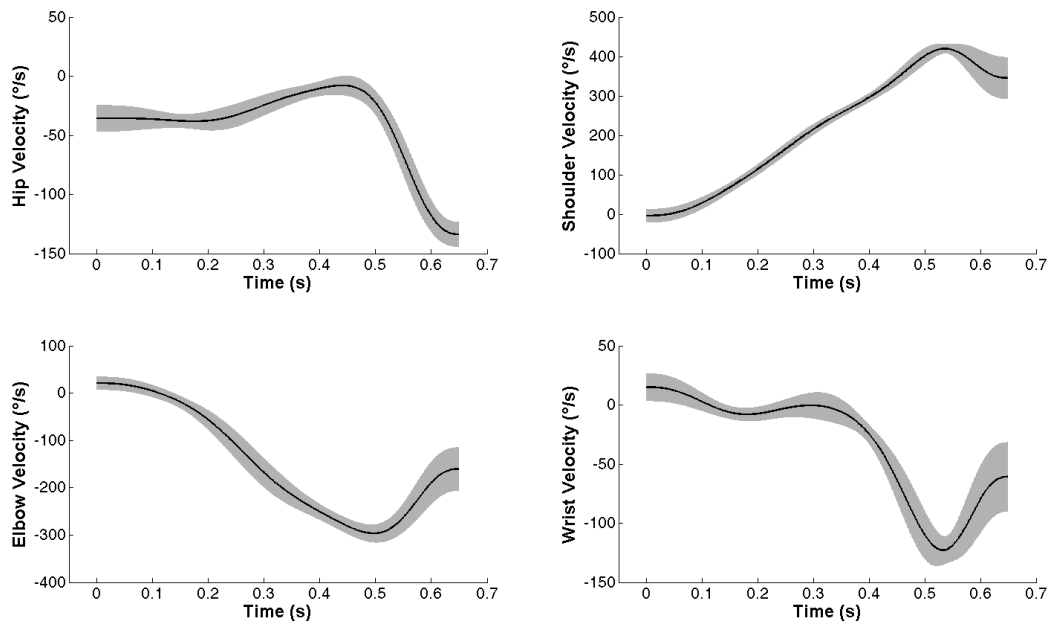
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255 **Figure 3** - The relative joint angles of the hip, shoulder, elbow, and wrist throughout the wheelchair
256 curling delivery. The quantities are presented as arithmetic means \pm 1 standard deviation over 14
257 consecutive deliveries.

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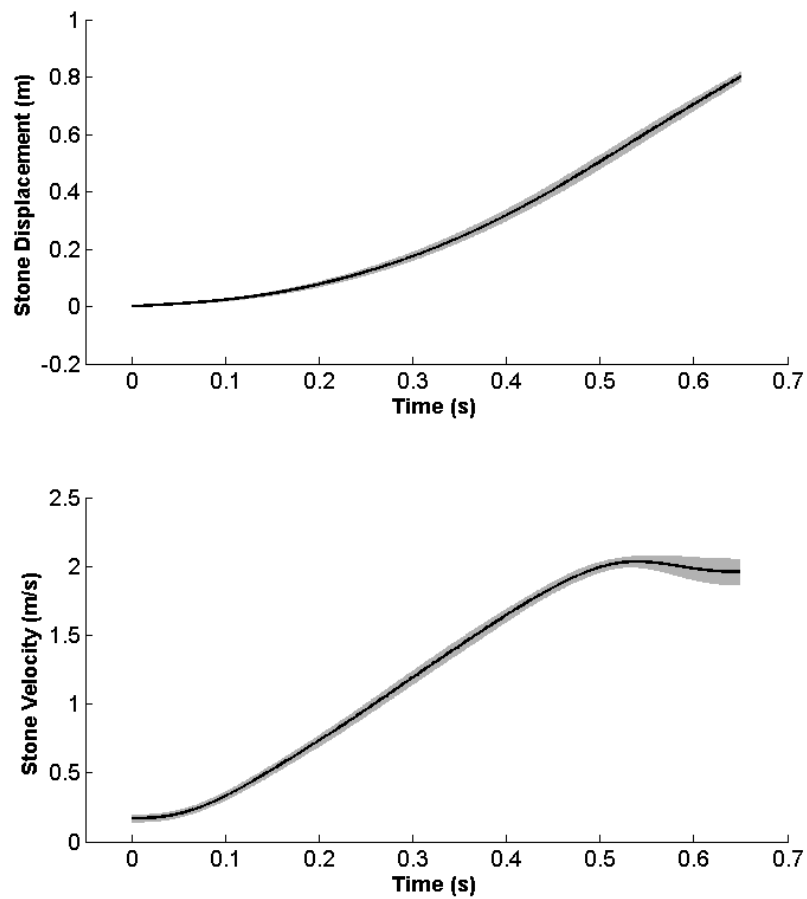
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262 **Figure 4** - The angular joint velocities of the hip, shoulder, elbow, and wrist throughout the wheelchair

263 curling delivery. The quantities are presented as arithmetic means \pm 1 standard deviation over 14

264 consecutive deliveries.

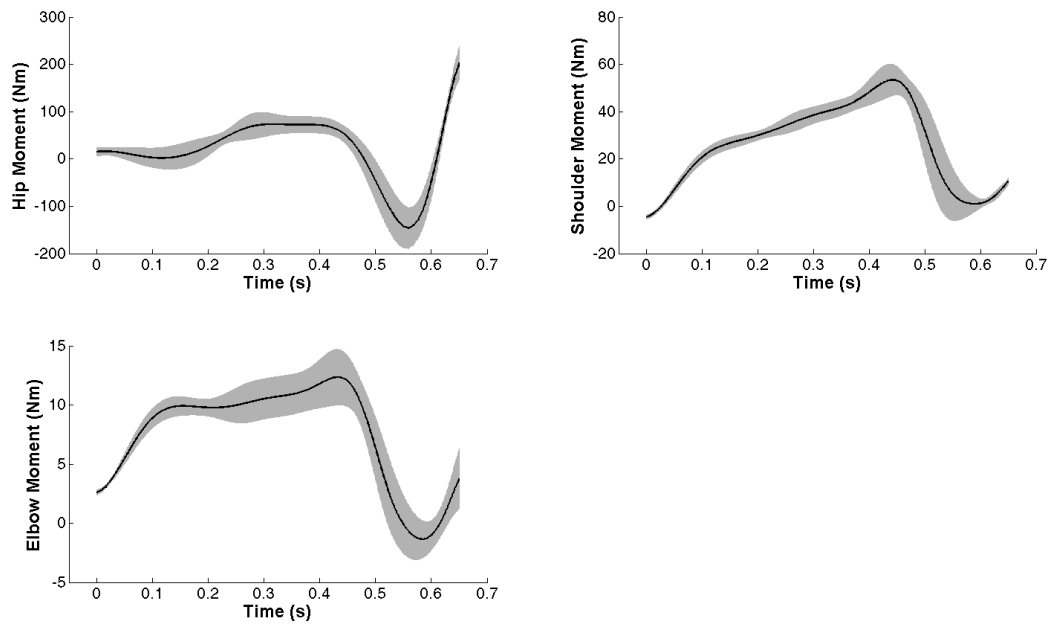
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267 **Figure 5** - The translational stone kinematics (i.e., displacements and velocities) throughout the
268 wheelchair curling delivery. The quantities are presented as arithmetic means \pm 1 standard deviation over
269 14 consecutive deliveries.

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Figure 6 - The resultant joint moments about the hip, shoulder, and elbow as computed via inverse dynamics analysis. The quantities are presented as arithmetic means \pm 1 standard deviation over 14 consecutive deliveries.